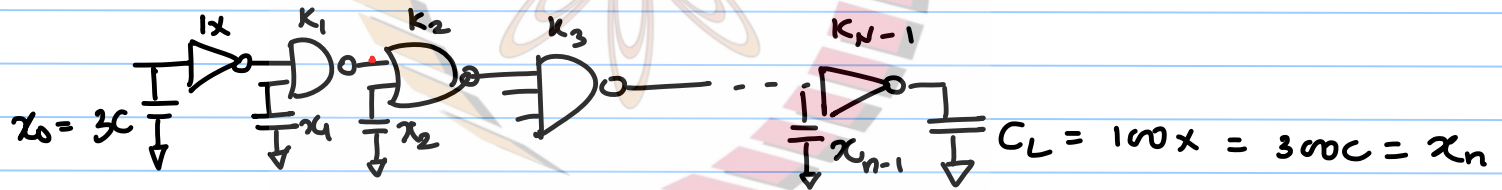


03/10/2019

EE5311

MODULE 4 - COMBINATIONAL CIRCUITS

GATE SIZING



$N \rightarrow \#$ of gates in the path.

$x_k \rightarrow$ I/O cap of the $(k+1)^{th}$ gate.

$$d_k = g_k h_k + p_k.$$

Minimize $d = \sum_{k=1}^N d_k$

$(x_1 \ x_2 \ \dots \ x_n)$

$d = \sum (g_k h_k + p_k) = \sum g_k h_k + \sum p_k$ \rightarrow not a fun of $(x_1 \ x_2 \ \dots \ x_n)$

$\min \sum g_k h_k.$

Let

$f_k = g_k h_k.$

$h_k = \frac{\text{O/P if } i}{\text{load cap}} = \frac{x_k}{x_{k-1}}$

$g_k = \text{ind of } (x_0 \ x_1 \ \dots \ x_n)$

$$\prod_{k=1}^N f_k = \prod g_k \cdot h_k = G H$$

$\prod_{k=1}^N g_k$

$\prod_{k=1}^N h_k$

$$G = \prod g_k = \text{Const number} = \text{PATH LOGICAL EFFORT}$$

$$H = \prod h_k = \frac{x_1}{x_0} \cdot \frac{x_2}{x_1} \cdot \dots \cdot \frac{x_N}{x_{N-1}} = \frac{x_N}{x_0} = \text{PATH ELECTRICAL EFFORT}$$



NOT a fn of $x_1 x_2 \dots x_{N-1}$

$$\min \sum f_k \quad \prod f_k = \text{Constant}$$

$$AM \geq GM \Rightarrow \frac{\sum_{k=1}^N f_k}{N} \geq \left(\prod_{k=1}^N f_k \right)^{1/N}$$

Soln to min problem.

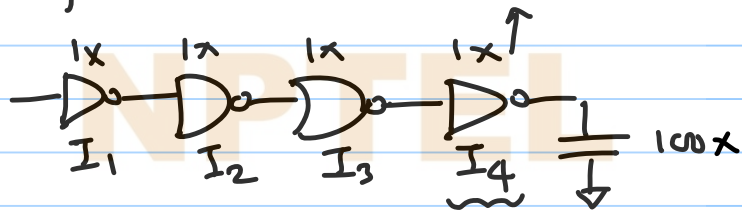
is $f_k = (GH)^{1/N}$

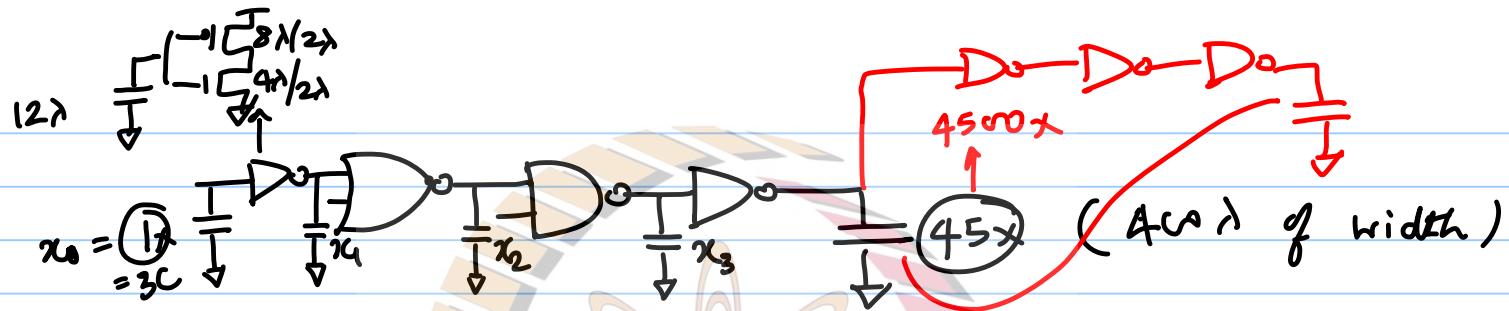
$\Rightarrow \sum f_k = N \cdot (GH)^{1/N}$

$\Rightarrow \text{min delay} = \sum f_k + \sum p_k = N (GH)^{1/N} + p$

Let $GH = F = \text{PATH EFFORT}$

$f_k = \text{STAGE EFFORT}$





g	①	$5/3$	$4/3$	1	$G = 20/9$
h	②	x_2/x_1	x_3/x_2	$45/x_3$	$H = O/P \text{ CAP} / I/P \text{ CAP} = 45$
p	1	2	2	1	$P = \sum p_k = 6$

$$(f_k \approx g_k) \quad x_1 \quad (5/3) \quad (x_2/x_1) \quad (4/3) \quad (x_3/x_2) \quad (45/x_3) = 3.14$$

$$F = G_1 H = 20/9 \times 45 = 100.$$

$$\text{OPTIMAL STAGE EFFORT} = (F)^{1/N} = (100)^{1/4} \approx \textcircled{3.14}$$

$$\Rightarrow \text{MIN DELAY} = N \cdot (F^{1/N}) + P = 18.6$$

$$f_k = 3.14$$

$$\frac{x_1}{1} = 3.14$$

$$\left(\frac{5}{3}\right)\left(\frac{x_2}{x_1}\right) = 3.14$$

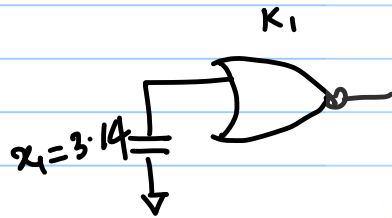
$$\Rightarrow x_2 = \frac{3}{5} \times 3.14 \times (3.14) = 6$$

$$\left(\frac{x_4}{x_3}\right) = 3.14$$

$$\left(\frac{45}{13.93}\right) \sim 3.14$$

$$\frac{4}{3} \times \frac{x_3}{x_2} = 3.14$$

$$\Rightarrow x_3 = \frac{3}{4} \times (3.14) \times 6 = 13.93$$



$$5 \cdot K_1 C = 3.14 \times 3C$$

$$\therefore K_1 = \frac{6 \times 3C}{5C} \Rightarrow K_1 = 3.6$$

NPTEL

$$G = 20/9$$

$$H = 4500$$

$$\Rightarrow F = (GH) = 10^4$$

$$\begin{aligned}\Rightarrow \text{MIN DELAY} &= N \cdot F^{1/N} + P \\ &= 4 \times (10^4)^{1/4} + 6 \\ &= 46\end{aligned}$$

$$\text{Stage effort} = f_k = F^{1/N} = 10$$

NPTEL