

Physics of Materials

- 1) A superconductor has a $B_C = \mu_0 H_{C2}$ value of 12 Teslas at 0 Kelvin. The material is therefore:
 - a) Definitely a metallic material
 - b) Definitely a ceramic material
 - c) A Type I superconductor
 - d) A Type II superconductor

- 2) A material ideally suited for opto-electronic applications is:
 - a) Si
 - b) GaAs
 - c) Ag
 - d) Cu

- 3) A boson is a particle that has the following characteristic
 - a) It has even number spin
 - b) It has half integer spin
 - c) It has three quarter integer spin
 - d) It has integer spin

- 4) In the classical description of materials, electronic contribution to the specific heat arises due to contributions from electrons that are
 - a) Close to the fermi energy
 - b) Just above the fermi energy
 - c) The bound electrons
 - d) All nearly free electrons

- 5) At brillouin zone boundaries,
 - a) The parabolic E Vs k relationship of nearly free electrons is maintained
 - b) The E Vs k relationship becomes linear
 - c) The E Vs k relationship becomes discontinuous
 - d) k is a minimum

- 6) In a p-type extrinsic semiconductor, the mobility of holes is
 - a) Independent of dopant concentration, at all levels of dopant concentration
 - b) Vastly greater than the mobility of electrons
 - c) Increases with increasing dopant concentration
 - d) Decreases with increasing dopant concentration

- 7) A material with strong ionic bonds displays:
 - a) A large bandgap between valence and conduction bands
 - b) A very small bandgap between valence and conduction bands
 - c) A half filled valence band
 - d) An overlap between valence and conduction bands

- 8) Phonons are:
 - a) Always optically active
 - b) Optically active in pure element solids

- c) Optically active in covalently bonded solids
- d) Optically active in ionically bonded solids

9) For a ferromagnetic material, χ has

- a) A large negative value
- b) A small negative value
- c) A small positive value
- d) A large positive value

10) The properties of a fine grained polycrystalline material that does not have any texture, but whose sample is in the shape of a cylinder, will be:

- a) Same in all directions
- b) Higher along the axial direction of the cylinder
- c) Higher along the radial direction
- d) Higher at 45° to the cylinder axis

11) A ceramic material with a large band gap is expected to be transparent because E_g for the material is such that the ν_{\min} is greater than that corresponding to UV radiation. However, samples of the same obtained commercially, were found to be opaque. What are the possible reasons for this? (List as many as you can)

12) A primitive hexagonal unit cell has the following specifications: $a = b = c$, $\alpha = \beta = 90^\circ$ and $\gamma = 120^\circ$. Draw the Wigner Seitz cell corresponding to this.

13) Briefly describe, using an appropriate diagram, the phase changes associated with Hume Rothery phases

14) The room temperature conductivity of a Si based sample, whose exact composition is not known, is $2 \times 10^3 (\Omega\text{m})^{-1}$. The hole concentration in this sample is $7 \times 10^{23} \text{ m}^{-3}$. The electron mobility and hole mobility in this material, at room temperature, are $0.14 \text{ m}^2/\text{Vs}$ and $0.05 \text{ m}^2/\text{Vs}$, respectively. What is the concentration of free electrons in this material? Is it intrinsic, n-type extrinsic, or p-type extrinsic?

15) A coil of Cu wire is such that the total length of the complete coil is 0.7 m. It has 250 turns within this length and carries a current of 10 A

- a) What is the magnetic field strength of the coil?
- b) What is the flux density of the coil in vacuum?
- c) If a bar of Ti is positioned within the coil, what will be the flux density within the bar.
- d) What is the magnitude of the Magnetization within the Ti bar in part (c) above?

$$\chi_m \text{ for Cu} = -0.96 \times 10^{-5}$$

$$\chi_m \text{ for Ti} = 1.81 \times 10^{-4}$$

$$\mu_0 = 1.257 \times 10^{-6} \text{ Webers/Am (same as Henries/m)}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ Farad/m}$$

18) The total energy of a KCl pair is given by:

$$E = (-e^2/4\pi\epsilon_0 R) + (B/R^{10}) + 8.00 \times 10^{-20} \quad \text{J}$$

What is the equilibrium spacing between the ions?

39) Assuming the classical free electron model, calculate the number of free electrons per cubic meter for silver. Assume that, on average, there are 1.4 free electrons per Ag atom. The electrical conductivity and density of Ag are $7 \times 10^7 (\Omega\text{m})^{-1}$ and 10.5 g/cm^3 , respectively. Also calculate the mobility of electrons in Ag

3)) Briefly explain, using appropriate diagrams, how the Sommerfeld model overcomes the limitation of the Drude model, with respect to estimating C_v^e

3)) Using a diagram, indicate the variation of resistivity of a well annealed pure metal, with temperature. On the same diagram show the variation of resistivity with temperature of the same metal after alloying it with another metal, the alloying addition being 5% and the alloy being a substitutional solid solution. Also on the same diagram, indicate the variation of resistivity with temperature of the same alloy after extensive plastic deformation. **It is sufficient of the diagram is a schematic diagram. The trend in each variation and relative positions of the variations are important.** Clearly indicate which curve/line represents each of the above cases.

42) At room temperature, the electrical conductivity for Silver is $7 \times 10^7 (\Omega\text{m})^{-1}$. Assume the electron mobility in Silver, at this temperature, is $3.0 \text{ m}^2/\text{Vs}$.

a) What is the number of free electrons per Silver atom?

b) Assuming the Wiedemann Franz law is obeyed, what is the thermal conductivity of Silver at room temperature (assume 30 C , and the Wiedemann Franz law constant to be $2.4 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$)

43) A hypothetical superconductor has a H_{c2} value of 1.5 T . What 'type' of super conductor is it? Explain your answer.

44) A Si based extrinsic semiconductor has a room temperature conductivity of $45 \Omega^{-1}\text{m}^{-1}$. Assuming $\mu_e = 0.05 \text{ m}^2/\text{V}$ and μ_h is $0.03 \text{ m}^2/\text{V}$, what concentration of a group VA dopant could have resulted in this? What concentration of a group IIIA dopant could have resulted in this? Assume material is in extrinsic region.

45) In the case of free electrons, energy is related to wave vector as indicated below:

$$E(k) = \hbar^2 k^2 / 2m$$

In the case of solids, this relationship breaks down, however its general form can be maintained using:

$$E(k) = \hbar^2 k^2 / 2m^*$$

Where m^* is an adjustable parameter, which we call the effective mass. The effective mass can be defined by:

$$m^* = \hbar^2 / (d^2E/dk^2)$$

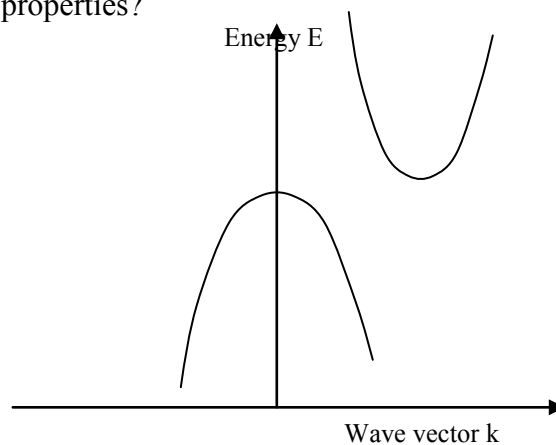
Assuming that the solid behaviour is consistent with free electrons subject to a weak periodic potential, **schematically plot** the variation of effective mass m^* as a function of wave vector in the first Brillouin zone, in the region that would correspond to the first band (assume a simple one dimensional lattice with lattice spacing 'a')

46) Make a plot (to scale) of the first two Brillouin zones for a rectangular two dimensional lattice which has unit vectors in the real space of along the x and y directions of $a = 0.2$ nm and $b = 0.4$ nm

47) A crystal has a real space lattice that has a unit cell defined by the vectors $(a/2)(i + j)$, $(a/2)(j + k)$, $(a/2)(k + i)$, where i, j, k , are unit vectors in three mutually perpendicular directions. What are the unit cell vectors corresponding to the reciprocal lattice of this real space lattice?

48) For Cu at 1000 K, if the Fermi energy is 7.06 eV, what is the energy at which the probability that an electron state will be occupied, is 70%? What is the probability of occupancy at the Fermi energy?

29) The band structure of a material is as shown below. What can you say about its use for its optical properties?



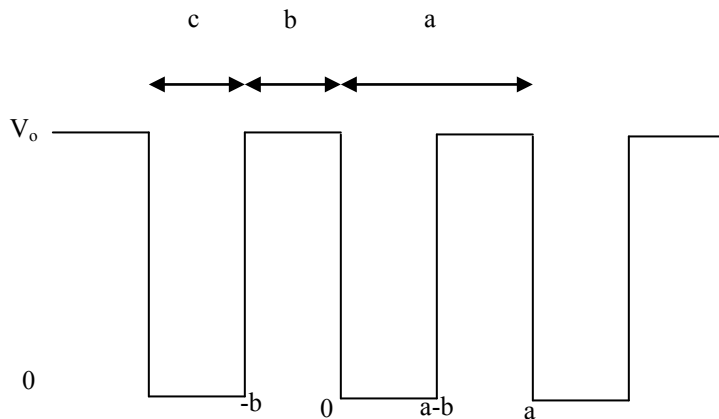
4:) From a reciprocal lattice perspective what can you say about the differences in diffraction patterns obtained from a single crystal using a typical laboratory X-ray diffraction

equipment and an electron microscope operating at 200 kV? (The crystal is mounted in the same fixed orientation in both cases with respect to incident beam)

29) When you construct the Wigner Seitz cell for an arbitrary two dimensional, periodic, lattice, what is the most general shape (number of sides) that will result? Under what conditions will the number of sides decrease relative to that obtained in the most general case.

30) Derive the expression for Bose-Einstein Statistics. Clearly show all steps, indicate all assumptions, and approximations and justify the same.

31) Assuming an electron experiences the simplified square periodic potential shown in the figure below, write and solve the Schrodinger wave equation for the regions where the potential is V_0 as well as for the regions where the potential is zero. Assuming Bloch periodicity condition is valid, what relationships can you expect between the solution at '-b' on the V_0 potential side, and the solution at 'a-b' on the potential 0 side? (expand the relationships completely, you need not write or solve the determinant)



32) Indicate using appropriate, fully labeled sketches, how paramagnetism is explained using the quantum mechanical nearly free electron theory.

33) What are Cooper pairs? What can you say about their \mathbf{k} vectors and spin?

34) How do Si and GaAs compare with respect to their potential use for opto-electronic applications. Explain using appropriate diagrams.

35) The top of the valence band of a hypothetical pure elemental semiconductor is at 4.4 eV, while the conduction band starts at 6.0 eV and the Fermi energy of the semiconductor is at 5.2 eV. What frequencies of light will be absorbed by this pure elemental semiconductor?

Mass of electron = 9.11×10^{-31} kg

Mass of proton = 1.67×10^{-27} kg

Charge on an electron = 1.6×10^{-19} C

Speed of light = 3×10^8 m/s

$h = 6.63 \times 10^{-34}$ Js

$k = 1.38 \times 10^{-23}$ J/K

Avogadro Constant = 6.02×10^{23} mol⁻¹