

# Vibrations of Structures

## Module V: Vibrations of Plates

### Exercises

1. A square plate of side  $a$  is simply-supported at the four edges, and carries a particle of mass  $m$  at the center. Determine the eigenfrequencies and eigenfunctions of the plate.
2. A circular plate of radius  $a$  is simply supported at the boundary. Determine the dynamic reaction forces at the boundary for different modes of vibration of the plate.
3. An elliptic plate of semi-major axis  $a$  and semi-minor axis  $b$  is simply supported at the boundary. Determine the approximate eigenfrequencies and modes of vibrations. Plot the variation of the first six eigenfrequencies with the ratio  $a/b$  in the range  $(1, 2)$ .

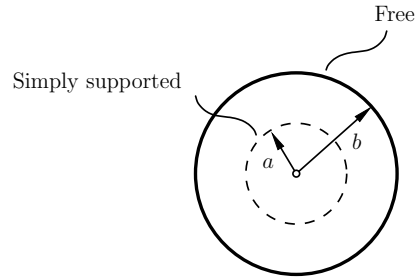


Figure 1: Exercise 4

4. A circular plate of radius  $a$  is simply-supported on a circle of radius  $b$ , as shown in Fig. 1. Determine the optimum ratio  $b/a$  for which the plate is most firmly supported in the mode  $(0, 1)$  (*i.e.*, the corresponding frequency is maximized).
5. A circular plate of radius  $a$  is clamped at the boundary  $r = a$ . A particle of mass  $m$  is dropped from a height  $h$  exactly on the center of the plate. The particle sticks to the plate. Determine the motion of the plate and the force between the particle and the plate.

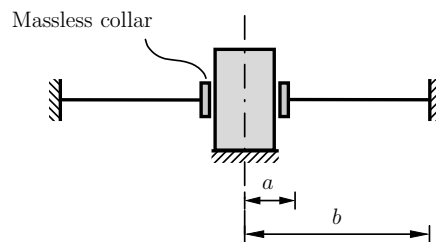


Figure 2: Exercise 6

6. An annular plate of inner radius  $a$  and outer radius  $b$  is clamped at the boundary  $r = b$ , and clamped to a massless collar (at  $r = a$ ) sliding without friction on a guide, as shown in Fig. 2. Determine the eigenfrequencies and eigenfunctions of the system. If the collar is excited by a harmonic force  $Q(t) = A \cos \Omega t$ , determine the response of the plate.

7. A circular plate of radius  $a$  is clamped at the boundary. A constant point force is traveling on a circular path around the center of the plate at a radius  $r_0$ , *i.e.*,  $q(r, \phi, t) = Q_0 \delta(r - r_0) \delta(\phi - \Omega t)$ , where  $Q_0$  is the constant magnitude, and  $\Omega$  is the angular speed. Determine the response of the plate. At what values of  $\Omega$  will the plate resonate?
8. A square plate of side  $a$  is simply supported at the edges on a rigid frame. The frame is given harmonic angular oscillations of circular frequency  $\Omega$  about a center line parallel to an edge. Determine the response of the plate.